

ANEXO 11: Cálculo de los Residuos

En este anexo se presentan las derivadas del potencial complejo para el modelo Clásico, SZ-I, SZ-II y SZ-III. Además, se resuelven los términos provenientes de $\left(\frac{dF}{dz}\right)^2$, aplicando el Teorema del Residuo (Murray, 1971; Hauser, 1973).

Modelo Clásico

$$\frac{dF}{dz} = V_o - V_o \frac{a^2}{z^2} - \frac{1}{2} i \frac{a^2}{z}$$

$$\left(\frac{dF}{dz}\right)^2 = V_o^2 - 2V_o^2 \frac{a^2}{z^2} - iV_o \frac{a^2}{z} - V_o^2 \frac{a^4}{z^4} - iV_o \frac{a^2}{z^3} - \frac{1}{4} \frac{a^2}{z^2}$$

Para a_1

$$f(z) = V_o^2$$

$$a_1 = 0$$

Para a_2

$$f(z) = -2V_o^2 \frac{a^2}{z^2}$$

$$R = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-2V_o^2 \frac{a^2}{z^2} \right) = 0$$

$$a_2 = 0$$

Para a_3

$$f(z) = iV_o \frac{a^2}{z}$$

$$R = \lim_{z \rightarrow 0} \frac{1}{z - 0} \left(iV_o \frac{a^2}{z} - iV_o \frac{a^2}{z} \right) = 0$$

$$a_3 = iV_o \frac{a^2}{z}$$

Para a_4

$$f(z) = V_o^2 \frac{a^4}{z^4}$$

$$R = \frac{1}{4-1!} \lim_{z \rightarrow 0} \frac{d^{4-1}}{dz^{4-1}} \left(z - 0 \right)^4 \left(V_o^2 \frac{a^4}{z^4} \right) = 0$$

$$a_4 = 0$$

Para a_5

$$f(z) = -iV_o \frac{a^2}{z^3} -$$

$$R = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0^3 \left(-iV_o \frac{a^2}{z^3} - \right) \right) = 0$$

$$a_5 = 0$$

Para a_6

$$f(z) = -\frac{1}{4} \frac{2}{z^2}$$

$$R = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^2 \left(-\frac{1}{4} \frac{2}{z^2} \right) \right) = 0$$

$$a_6 = 0$$

Modelo SZ-I

$$\frac{dF}{dz} = V_o - V_o \frac{a^2}{z^2} - \frac{1}{2} i \frac{Q}{z} - \frac{1}{2} \frac{Q}{(z-be^i)} - \frac{1}{2} Q \frac{b}{(zb-a^2e^i)} - \frac{1}{2} \frac{Q}{z}$$

$$\begin{aligned} \left(\frac{dF}{dz} \right)^2 &= \frac{1}{4} \frac{Q^2}{z^2(z-be^i)^2} - \frac{1}{4} \frac{2}{z^2} - 2V_o^2 \frac{a^2}{z^2} - V_o^2 \frac{a^4}{z^4} \\ &+ \frac{1}{4} \frac{Q^2}{z^2} - V_o^2 - iV_o \frac{a^2}{z^3} - V_o \frac{a^2}{z^3} \frac{Q}{z} - \frac{1}{2} i \frac{Q}{z^2} Q - \frac{Q}{(z-be^i)} V_o - \frac{Q}{(z-be^i)} V_o \frac{a^2}{z^2} - \frac{1}{2} i \frac{Q}{z^2(z-be^i)} \\ &- \frac{1}{z} - \frac{1}{2} \frac{Q^2}{z^2(z-be^i)} \frac{b}{zb-a^2e^i} - \frac{1}{2} \frac{Q^2}{z^2(z-be^i)_z} - Q \frac{b}{(zb-a^2e^i)} V_o - Q \frac{b}{(zb-a^2e^i)} V_o \\ &\frac{a^2}{z^2} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i)} - \frac{1}{4} Q^2 \frac{b^2}{z^2(zb-a^2e^i)^2} - \frac{1}{2} Q^2 \frac{b}{z^2(zb-a^2e^i)_z} - iV_o \frac{Q}{z} - V_o \frac{Q}{z} \end{aligned}$$

Para a_1

$$f(z) = \frac{1}{4} \frac{Q^2}{z^2(z-be^i)^2}$$

$$a_1 = 0$$

Para a_2

$$f(z) = -\frac{1}{4} \frac{2}{z^2}$$

$$\text{Res}_{z=0} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-\frac{1}{4} \frac{2}{z^2} \right) = 0$$

$$a_2 = 0$$

Para a_3

$$f(z) = -2V_o^2 \frac{a^2}{z^2}$$

$$\text{Res}_{z=0} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-2V_o^2 \frac{a^2}{z^2} \right) = 0$$

$$a_3 = 0$$

Para a_4

$$f(z) = V_o^2 \frac{a^4}{z^4}$$

$$\text{Res}_{z=0} \frac{1}{4-1!} \lim_{z \rightarrow 0} \frac{d^{4-1}}{dz^{4-1}} \left(z - 0 \right)^4 \left(V_o^2 \frac{a^4}{z^4} \right) = 0$$

$$a_4 = 0$$

Para a_5

$$f(z) = \frac{1}{4} \frac{Q^2}{z^2}$$

$$\text{Res}_{z=0} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(\frac{1}{4} \frac{Q^2}{z^2} \right) = 0$$

$$a_5 = 0$$

Para a_6

$$f(z) = V_o^2$$

$$a_6 = 0$$

Para a_7

$$f(z) = -iV_o \frac{a^2}{z^3} -$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0^3 \left(-iV_o \frac{a^2}{z^3} - \right) \right) = 0$$

$$a_7 = 0$$

Para a_8

$$f(z) = V_o \frac{a^2}{z^3} \frac{Q}{z}$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0^3 \left(V_o \frac{a^2}{z^3} \frac{Q}{z} \right) \right) = 0$$

$$a_8 = 0$$

Para a_9

$$f(z) = -\frac{1}{2}i \frac{Q}{z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^2 \left(-\frac{1}{2}i \frac{Q}{z^2} \right) \right) = 0$$

$$a_9 = 0$$

Para a_{10}

$$f(z) = \frac{Q}{(z-be^i)} V_o$$

$$a_{10} = 0$$

Para a_{11}

$$f(z) = -\frac{Q}{(z-be^i)} V_o \frac{a^2}{z^2}$$

$$\text{Res} \quad \frac{1}{2-1} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^2 \left(-\frac{Q}{(z-be^i)} V_o \frac{a^2}{z^2} \right) \right) = \frac{1}{b^2 e^{2i}} V_o a^2 \frac{Q}{2}$$

$$a_{11} = \frac{1}{b^2 e^{2i}} V_o a^2 \frac{Q}{2}$$

Para a_{12}

$$f(z) = \frac{1}{2} i \frac{Q}{z^2 (z-be^i)} \frac{1}{z}$$

$$\text{Res} \quad \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i \frac{Q}{z^2 (z-be^i)} \frac{1}{z} \right) \right) = -\frac{1}{2} \frac{i}{be^i} \frac{Q}{2}$$

$$a_{12} = -\frac{1}{2} \frac{i}{be^i} \frac{Q}{2}$$

Para a_{13}

$$f(z) = \frac{1}{2} \frac{Q^2}{z^2 (z-be^i)} \frac{b}{zb-a^2 e^i}$$

$$\text{Res} \quad \lim_{z \rightarrow \frac{a^2 e^i}{b}} \left(\left(z - \frac{a^2 e^i}{b} \right) \left(\frac{1}{2} \frac{Q^2}{z^2 (z-be^i)} \frac{b}{zb-a^2 e^i} \right) \right) = -\frac{1}{2e^i} \frac{1}{-a^2 b^2} \frac{Q^2}{2} b$$

$$a_{13} = -\frac{1}{2e^i} \frac{1}{-a^2 b^2} \frac{Q^2}{2} b$$

Para a_{14}

$$f(z) = -\frac{1}{2} \frac{Q^2}{z^2 (z-be^i)} \frac{1}{z}$$

$$\text{Res} \quad \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} \frac{Q^2}{z^2 (z-be^i)} \frac{1}{z} \right) \right) = \frac{1}{2be^i} \frac{Q^2}{2}$$

$$a_{14} = \frac{1}{2be^i} \frac{Q^2}{2}$$

Para a_{15}

$$f(z) = Q \frac{b}{(zb-a^2 e^i)} V_o$$

$$\text{Res} \lim_z \frac{a^2 e^i}{b} \left(\left(z - \frac{a^2 e^i}{b} \right) \left(Q \frac{b}{(zb - a^2 e^i)} V_o \right) \right) = \underline{Q} V_o$$

$$a_{15} = \underline{Q} V_o$$

Para a_{16}

$$f(z) = -Q \frac{b}{(zb - a^2 e^i)} V_o \frac{a^2}{z^2}$$

$$\text{Res}_1 \lim_z \frac{a^2 e^i}{b} \left(\left(z - \frac{a^2 e^i}{b} \right) \left(-Q \frac{b}{(zb - a^2 e^i)} V_o \frac{a^2}{z^2} \right) \right) = -\frac{b^2}{a^2 e^{2i}} \underline{Q} V_o$$

$$\text{Res}_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-Q \frac{b}{(zb - a^2 e^i)} V_o \frac{a^2}{z^2} \right) = \frac{b^2}{a^2 e^{2i}} \underline{Q} V_o$$

$$a_{16} = \text{Res}_1 - \text{Res}_2 = 0$$

Para a_{17}

$$f(z) = \frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^i)} \frac{1}{z}$$

$$\text{Res}_1 \lim_z \frac{a^2 e^i}{b} \left(\left(z - \frac{a^2 e^i}{b} \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^i)} \frac{1}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^i} Q \frac{b}{2}$$

$$\text{Res}_2 \lim_{z \rightarrow 0} \left(z - 0 \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^i)} \frac{1}{z} \right) = -\frac{1}{2} \frac{i}{a^2 e^i} Q \frac{b}{2}$$

$$a_{17} = \text{Res}_1 - \text{Res}_2 = 0$$

Para a_{18}

$$f(z) = \frac{1}{4} Q^2 \frac{b^2}{z^2 (zb - a^2 e^i)^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_z \frac{a^2 e^i}{b} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^i}{b} \right)^2 \left(\frac{1}{4} Q^2 \frac{b^2}{z^2 (zb - a^2 e^i)^2} \right) \right) = 0$$

$$a_{18} = 0$$

Para a_{19}

$$f(z) = -\frac{1}{2}Q^2 \frac{b}{(zb-a^2e^i)^2 z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2e^i}{b}} \left(\left(z - \frac{a^2e^i}{b} \right) \left(-\frac{1}{2}Q^2 \frac{b}{(zb-a^2e^i)^2 z} \right) \right) = -\frac{1}{2a^2e^i}Q^2 \frac{b}{2}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2}Q^2 \frac{b}{(zb-a^2e^i)^2 z} \right) \right) = \frac{1}{2a^2e^i}Q^2 \frac{b}{2}$$

$$a_{19} = Res_1 + Res_2 = 0$$

Para a_{20}

$$f(z) = iV_o \frac{1}{z}$$

$$Res = \lim_{z \rightarrow 0} \left(z - 0 \right) iV_o \frac{1}{z} = iV_o$$

$$a_{20} = iV_o$$

Para a_{21}

$$f(z) = -V_o \frac{Q}{z}$$

$$Res = \lim_{z \rightarrow 0} \left(z - 0 \right) \left(-V_o \frac{Q}{z} \right) = -\frac{Q}{V_o}$$

$$a_{21} = -\frac{Q}{V_o}$$

Modelo SZ-II

$$\frac{dF}{dz} = V_o - V_o \frac{a^2}{z^2} - \frac{1}{2}i \frac{1}{z} - \frac{1}{2} \frac{Q}{(z-be^i)^2} - \frac{1}{2}Q \frac{b}{(zb-a^2e^i)^2} - \frac{Q}{z} - \frac{1}{2} \frac{Q}{(z-be^i)^2}$$

$$\left(\frac{dF}{dz} \right)^2 = \left(V_o - V_o \frac{a^2}{z^2} - \frac{1}{2}i \frac{1}{z} - \frac{1}{2} \frac{Q}{(z-be^i)^2} - \frac{1}{2}Q \frac{b}{(zb-a^2e^i)^2} - \frac{Q}{z} - \frac{1}{2} \frac{Q}{(z-be^i)^2} \right)^2 - 2V_o^2 \frac{a^2}{z^2} - \frac{1}{4} \frac{1}{z^2} - \frac{1}{4} \frac{Q^2}{(z-be^i)^2} - \frac{1}{4} \frac{Q^2}{(z-be^i)^2} - \frac{Q^2}{2z^2} - V_o^2 \frac{a^4}{z^4} - iV_o \frac{a^2}{z^3} - 2V_o \frac{a^2}{z^3} \frac{Q}{z} - i \frac{1}{2z^2} Q - \frac{Q}{(z-be^i)^2} V_o - \frac{Q}{(z-be^i)^2} V_o \frac{a^2}{z^2} - \frac{1}{2}i \frac{Q}{(z-be^i)^2} \frac{1}{z} - \frac{1}{2} \frac{Q^2}{(z-be^i)^2}$$

$$\begin{aligned}
& \frac{b}{zb-a^2e^{i p}} - \frac{Q^2}{2(z-be^{i p})z} \quad \frac{1}{2} \frac{Q^2}{2(z-be^{i p})(z-be^{i n})} \quad \frac{1}{2} \frac{Q^2}{2(z-be^{i p})} \frac{b}{zb-a^2e^{i n}} \quad Q \frac{b}{(zb-a^2e^{i p})} \\
V_o - Q \frac{b}{(zb-a^2e^{i p})} V_o \frac{a^2}{z^2} & \quad \frac{1}{2} i Q \frac{b}{2(zb-a^2e^{i p})} \frac{1}{z} \quad \frac{1}{4} Q^2 \frac{b^2}{2(zb-a^2e^{i p})^2} - Q^2 \frac{b}{2(zb-a^2e^{i p})z} \\
\frac{1}{2} Q^2 \frac{b}{2(zb-a^2e^{i p})(z-be^{i n})} & \quad \frac{1}{2} Q^2 \frac{b^2}{2(zb-a^2e^{i p})(zb-a^2e^{i n})} \quad \frac{Q}{(z-be^{i n})} V_o - \frac{Q}{(z-be^{i n})} V_o \frac{a^2}{z^2} \quad \frac{1}{2} \\
i \frac{Q}{2(z-be^{i n})} \frac{1}{z} - \frac{Q^2}{2(z-be^{i n})z} & \quad \frac{1}{2} \frac{Q^2}{2(z-be^{i n})} \frac{b}{zb-a^2e^{i n}} \quad Q \frac{b}{(zb-a^2e^{i n})} \\
V_o - Q \frac{b}{(zb-a^2e^{i n})} V_o \frac{a^2}{z^2} & \quad \frac{1}{2} i Q \frac{b}{2(zb-a^2e^{i n})} \frac{1}{z} - Q^2 \frac{b}{2(zb-a^2e^{i n})z} \quad \frac{1}{4} Q^2 \frac{b^2}{2(zb-a^2e^{i n})^2} \\
iV_o \frac{1}{z} - 2V_o \frac{Q}{z} & \quad V_o^2
\end{aligned}$$

Para a_1

$$f(z) = -2V_o^2 \frac{a^2}{z^2}$$

$$Res_{z=0} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-2V_o^2 \frac{a^2}{z^2} \right) = 0$$

$$a_1 = 0$$

Para a_2

$$f(z) = -\frac{1}{4} \frac{2}{z^2}$$

$$Res_{z=0} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-\frac{1}{4} \frac{2}{z^2} \right) = 0$$

$$a_2 = 0$$

Para a_3

$$f(z) = \frac{1}{4} \frac{Q^2}{2(z-be^{i n})^2}$$

$$a_3 = 0$$

Para a_4

$$f(z) = \frac{1}{4} \frac{Q^2}{2(z-be^{i p})^2}$$

$$a_4 = 0$$

Para a_5

$$f(z) = \frac{Q^2}{2z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(\frac{Q^2}{2z^2} \right) = 0$$

$$a_5 = 0$$

Para a_6

$$f(z) = V_o^2 \frac{a^4}{z^4}$$

$$\text{Res} = \frac{1}{4-1!} \lim_{z \rightarrow 0} \frac{d^{4-1}}{dz^{4-1}} \left(z - 0 \right)^4 \left(V_o^2 \frac{a^4}{z^4} \right) = 0$$

$$a_6 = 0$$

Para a_7

$$f(z) = -iV_o \frac{a^2}{z^3} -$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0 \right)^3 \left(-iV_o \frac{a^2}{z^3} - \right) = 0$$

$$a_7 = 0$$

Para a_8

$$f(z) = 2V_o \frac{a^2}{z^3} \frac{Q}{z}$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0 \right)^3 \left(2V_o \frac{a^2}{z^3} \frac{Q}{z} \right) = 0$$

$$a_8 = 0$$

Para a_9

$$f(z) = -i \frac{Q}{2z^2}$$

$$\text{Res} = \frac{1}{2-1} \lim_{z \rightarrow 0} z \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-i \frac{Q}{2z^2} \right) = 0$$

$$a_9 = 0$$

Para a_{10}

$$f(z) = \frac{Q}{(z - be^{i\phi})} V_o$$

$$a_{10} = 0$$

Para a_{11}

$$f(z) = -\frac{Q}{(z - be^{i\phi})} V_o \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1} \lim_{z \rightarrow 0} z \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-\frac{Q}{(z - be^{i\phi})} V_o \frac{a^2}{z^2} \right) = \frac{1}{b^2 e^{2i\phi}} V_o a^2 \frac{Q}{2}$$

$$a_{11} = \frac{1}{b^2 e^{2i\phi}} V_o a^2 \frac{Q}{2}$$

Para a_{12}

$$f(z) = \frac{1}{2} i \frac{Q}{z^2 (z - be^{i\phi})} \frac{1}{z}$$

$$\text{Res} = \lim_{z \rightarrow 0} z \left(z - 0 \right) \left(\frac{1}{2} i \frac{Q}{z^2 (z - be^{i\phi})} \frac{1}{z} \right) = -\frac{1}{2} \frac{i}{be^{i\phi}} \frac{Q}{2}$$

$$a_{12} = -\frac{1}{2} \frac{i}{be^{i\phi}} \frac{Q}{2}$$

Para a_{13}

$$f(z) = \frac{1}{2} \frac{Q^2}{z^2 (z - be^{i\phi})} \frac{b}{zb - a^2 e^{i\phi}}$$

$$\text{Res} \lim_z \frac{a^2 e^{i p}}{b} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(\frac{1}{2} \frac{Q^2}{(z - b e^{i p})} \frac{b}{z b - a^2 e^{i p}} \right) \right) = \frac{1}{2 e^{i p} a^2 - b^2} \frac{Q^2}{2} b$$

$$a_{13} = \frac{1}{2 e^{i p} a^2 - b^2} \frac{Q^2}{2} b$$

Para a_{14}

$$f(z) = -\frac{Q^2}{2(z - b e^{i p})z}$$

$$\text{Res} \lim_z 0 \left(z - 0 \left(-\frac{Q^2}{2(z - b e^{i p})z} \right) \right) = \frac{1}{b e^{i p}} \frac{Q^2}{2}$$

$$a_{14} = \frac{1}{b e^{i p}} \frac{Q^2}{2}$$

Para a_{15}

$$f(z) = \frac{1}{2} \frac{Q^2}{(z - b e^{i p})(z - b e^{i n})}$$

$$a_{15} = 0$$

Para a_{16}

$$f(z) = \frac{1}{2} \frac{Q^2}{(z - b e^{i p})} \frac{b}{z b - a^2 e^{i n}}$$

$$\text{Res} \lim_z \frac{a^2 e^{i n}}{b} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(\frac{1}{2} \frac{Q^2}{(z - b e^{i p})} \frac{b}{z b - a^2 e^{i n}} \right) \right) = \frac{1}{2(a^2 e^{i n} - e^{i p} b^2)} \frac{Q^2}{2} b$$

$$a_{16} = \frac{1}{2(a^2 e^{i n} - e^{i p} b^2)} \frac{Q^2}{2} b$$

Para a_{17}

$$f(z) = Q \frac{b}{(z b - a^2 e^{i p})} V_o$$

$$\text{Res} \lim_z \frac{a^2 e^{i p}}{b} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(Q \frac{b}{(z b - a^2 e^{i p})} V_o \right) \right) = \underline{Q} V_o$$

$$a_{17} = \frac{Q}{V_o}$$

Para a_{18}

$$f(z) = -Q \frac{b}{(zb - a^2 e^{i p})} V_o \frac{a^2}{z^2}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(-Q \frac{b}{(zb - a^2 e^{i p})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{b^2}{a^2 e^{2 i p}} \frac{Q}{V_o}$$

$$Res_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-Q \frac{b}{(zb - a^2 e^{i p})} V_o \frac{a^2}{z^2} \right) = \frac{b^2}{a^2 e^{2 i p}} \frac{Q}{V_o}$$

$$a_{18} = Res_1 - Res_2 = 0$$

Para a_{19}

$$f(z) = \frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i p})^2} \frac{1}{z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(\frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i p})^2} \frac{1}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i p}} Q \frac{b}{2}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \right) \left(\frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i p})^2} \frac{1}{z} \right) = -\frac{1}{2} \frac{i}{a^2 e^{i p}} Q \frac{b}{2}$$

$$a_{19} = Res_1 - Res_2 = 0$$

Para a_{20}

$$f(z) = \frac{1}{4} Q^2 \frac{b^2}{(zb - a^2 e^{i p})^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right)^2 \left(\frac{1}{4} Q^2 \frac{b^2}{(zb - a^2 e^{i p})^2} \right) \right) = 0$$

$$a_{20} = 0$$

Para a_{21}

$$f(z) = -Q^2 \frac{b}{2(zb - a^2 e^{i p})z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(-Q^2 \frac{b}{2(zb - a^2 e^{i p})z} \right) \right) = -\frac{1}{a^2 e^{i p}} Q^2 \frac{b}{2}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(-Q^2 \frac{b}{2(zb - a^2 e^{i p})z} \right) \right) = \frac{1}{a^2 e^{i p}} Q^2 \frac{b}{2}$$

$$a_{21} = Res_1 + Res_2 = 0$$

Para a_{22}

$$f(z) = \frac{1}{2} Q^2 \frac{b}{2(zb - a^2 e^{i p})(z - b e^{i n})}$$

$$Res = \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(\frac{1}{2} Q^2 \frac{b}{2(zb - a^2 e^{i p})(z - b e^{i n})} \right) \right) = \frac{1}{2(a^2 e^{i p} - b^2 e^{i n})} Q^2 \frac{b}{2}$$

$$a_{22} = \frac{1}{2(a^2 e^{i p} - b^2 e^{i n})} Q^2 \frac{b}{2}$$

Para a_{23}

$$f(z) = \frac{1}{2} Q^2 \frac{b^2}{2(zb - a^2 e^{i p})(zb - a^2 e^{i n})}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{b}} \left(\left(z - \frac{a^2 e^{i p}}{b} \right) \left(\frac{1}{2} Q^2 \frac{b^2}{2(zb - a^2 e^{i p})(zb - a^2 e^{i n})} \right) \right) = \frac{1}{2} \frac{b}{a^2 (e^{i p} - e^{i n})} \frac{Q^2}{2}$$

$$Res_2 = \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(\frac{1}{2} Q^2 \frac{b^2}{2(zb - a^2 e^{i p})(zb - a^2 e^{i n})} \right) \right) = -\frac{1}{2} \frac{b}{a^2 (e^{i p} - e^{i n})} \frac{Q^2}{2}$$

$$a_{23} = Res_1 + Res_2 = 0$$

Para a_{24}

$$f(z) = \frac{Q}{(z - b e^{i n})} V_o$$

$$a_{24} = 0$$

Para a_{25}

$$f(z) = -\frac{Q}{(z-be^{in})} V_o \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(-\frac{Q}{(z-be^{in})} V_o \frac{a^2}{z^2} \right) \right) = \frac{1}{b^2 e^{2in}} \frac{Q}{2} V_o a^2$$

$$a_{25} = \frac{1}{b^2 e^{2in}} \frac{Q}{2} V_o a^2$$

Para a_{26}

$$f(z) = \frac{1}{2} i \frac{Q}{z^2 (z-be^{in})} \frac{1}{z}$$

$$\text{Res} = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i \frac{Q}{z^2 (z-be^{in})} \frac{1}{z} \right) \right) = -\frac{1}{2} \frac{i}{be^{in}} \frac{Q}{2}$$

$$a_{26} = -\frac{1}{2} \frac{i}{be^{in}} \frac{Q}{2}$$

Para a_{27}

$$f(z) = -\frac{Q^2}{z^2 (z-be^{in}) z}$$

$$\text{Res} = \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{Q^2}{z^2 (z-be^{in}) z} \right) \right) = \frac{1}{be^{in}} \frac{Q^2}{2}$$

$$a_{27} = \frac{1}{be^{in}} \frac{Q^2}{2}$$

Para a_{28}

$$f(z) = \frac{1}{2} \frac{Q^2}{z^2 (z-be^{in})} \frac{b}{zb-a^2 e^{in}}$$

$$\text{Res} = \lim_{z \rightarrow \frac{a^2 e^{in}}{b}} \left(\left(z - \frac{a^2 e^{in}}{b} \right) \left(\frac{1}{2} \frac{Q^2}{z^2 (z-be^{in})} \frac{b}{zb-a^2 e^{in}} \right) \right) = \frac{1}{2e^{in} a^2 - b^2} \frac{Q^2}{2} b$$

$$a_{28} = \frac{1}{2e^{in} a^2 - b^2} \frac{Q^2}{2} b$$

Para a_{29}

$$f(z) = Q \frac{b}{(zb - a^2 e^{i n})} V_o$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(Q \frac{b}{(zb - a^2 e^{i n})} V_o \right) \right) = \frac{Q}{b} V_o$$

$$a_{29} = \frac{Q}{b} V_o$$

Para a_{30}

$$f(z) = -Q \frac{b}{(zb - a^2 e^{i n})} V_o \frac{a^2}{z^2}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(-Q \frac{b}{(zb - a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{b^2}{a^2 e^{2 i n}} \frac{Q}{b} V_o$$

$$Res_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-Q \frac{b}{(zb - a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) = \frac{b^2}{a^2 e^{2 i n}} \frac{Q}{b} V_o$$

$$a_{30} = Res_1 - Res_2 = 0$$

Para a_{31}

$$f(z) = \frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i n})} \frac{1}{z}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(\frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i n})} \frac{1}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i n}} Q \frac{b}{2}$$

$$Res_2 \lim_{z \rightarrow 0} \left(z - 0 \right) \left(\frac{1}{2} i Q \frac{b}{(zb - a^2 e^{i n})} \frac{1}{z} \right) = -\frac{1}{2} \frac{i}{a^2 e^{i n}} Q \frac{b}{2}$$

$$a_{31} = Res_1 - Res_2 = 0$$

Para a_{32}

$$f(z) = -Q^2 \frac{b}{(zb - a^2 e^{i n})} \frac{1}{z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right) \left(-Q^2 \frac{b}{2(zb - a^2 e^{i n})z} \right) \right) = -\frac{1}{a^2 e^{i n}} Q^2 \frac{b}{2}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(-Q^2 \frac{b}{2(zb - a^2 e^{i n})z} \right) \right) = \frac{1}{a^2 e^{i n}} Q^2 \frac{b}{2}$$

$$a_{32} = Res_1 + Res_2 = 0$$

Para a_{33}

$$f(z) = \frac{1}{4} Q^2 \frac{b^2}{2(zb - a^2 e^{i n})^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow \frac{a^2 e^{i n}}{b}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i n}}{b} \right)^2 \left(\frac{1}{4} Q^2 \frac{b^2}{2(zb - a^2 e^{i n})^2} \right) \right) = 0$$

$$a_{33} = 0$$

Para a_{34}

$$f(z) = iV_o \frac{1}{z}$$

$$Res = \lim_{z \rightarrow 0} \left(z - 0 \right) iV_o \frac{1}{z} = iV_o$$

$$a_{34} = iV_o$$

Para a_{35}

$$f(z) = -2V_o \frac{Q}{z}$$

$$Res = \lim_{z \rightarrow 0} \left(z - 0 \right) \left(-2V_o \frac{Q}{z} \right) = -2QV_o$$

$$a_{35} = -2QV_o$$

Para a_{36}

$$f(z) = V_o^2$$

Modelo SZ-III

$$\begin{aligned} \frac{dF}{dz} z &= V_o - V_o \frac{a^2}{z^2} - \frac{1}{2} i \frac{1}{z} - \frac{1}{2} \frac{Q}{(z-be^i ab)} - \frac{1}{2} Q \frac{b}{(zb-a^2e^i ab)} - \frac{1}{2} \frac{Q}{z} - \frac{1}{2} i \frac{1}{(z-R_1e^i p)} \\ &+ \frac{1}{2} i \frac{1}{(zR_1-a^2e^i n)} - \frac{1}{2} i \frac{1}{(z-R_1e^i n)} - \frac{1}{2} i \frac{1}{(zR_1-a^2e^i p)} - \frac{1}{2} i \frac{2}{(zR_2e^i n)} - \frac{1}{2} i \frac{2}{(zR_2a^2e^i p)} \\ &- \frac{1}{2} i \frac{2}{(zR_2e^i p)} - \frac{1}{2} i R_2 \frac{2}{(zR_2a^2e^i n)} \end{aligned}$$

$$\begin{aligned} \left(\frac{dF}{dz} z\right)^2 &= V_o^2 \frac{a^4}{z^4} - i \frac{2}{(zR_2e^i p)} V_o - \frac{1}{2} i \frac{2}{z^2} Q V_o \\ &+ \frac{a^2}{z^3} Q - i V_o \frac{a^2}{z^3} - V_o^2 - 2V_o^2 \frac{a^2}{z^2} - \frac{1}{4} \frac{Q^2}{z^2(z-be^i ab)^2} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} R_2 \frac{2}{zR_2a^2e^i n} \\ &+ Q \frac{b}{(zb-a^2e^i ab)} V_o - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} - \frac{1}{4} Q^2 \frac{b^2}{z^2(zb-a^2e^i ab)^2} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \\ &+ \frac{2}{zR_2e^i p} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{1}{z-R_1e^i n} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{1}{zR_1-a^2e^i p} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{1}{zR_1-a^2e^i n} \\ &+ \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{2}{zR_2e^i n} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{2}{zR_2a^2e^i p} - \frac{1}{2} \frac{Q^2}{z^2(z-be^i ab)} \frac{b}{zb-a^2e^i ab} - \\ &+ \frac{1}{2} \frac{Q^2}{z^2(z-be^i ab)z} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{1}{z-R_1e^i p} - \frac{Q}{(z-be^i ab)} V_o - \frac{Q}{(z-be^i ab)} \\ &+ V_o \frac{a^2}{z^2} - \frac{1}{2} i \frac{Q}{z^2(z-be^i ab)} \frac{1}{z} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{1}{zR_1-a^2e^i n} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \\ &+ \frac{1}{zR_1-a^2e^i p} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{2}{zR_2e^i n} - \frac{1}{2} Q^2 \frac{b}{z^2(zb-a^2e^i ab)z} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{1}{z-R_1e^i p} - Q \\ &+ \frac{b}{(zb-a^2e^i ab)} V_o \frac{a^2}{z^2} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{1}{z-R_1e^i n} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{2}{zR_2e^i p} \\ &+ \frac{R_2}{zR_2a^2e^i p} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} \frac{2}{zR_2e^i p} - \frac{1}{2} i Q \frac{b}{z^2(zb-a^2e^i ab)} R_2 \frac{2}{zR_2a^2e^i n} - \frac{1}{4} \frac{Q^2}{z^2} - \frac{1}{2} \frac{2}{z^2(z-R_1e^i p)} \\ &+ \frac{R_1}{zR_1-a^2e^i n} - \frac{1}{2} \frac{2}{z^2(z-R_1e^i p)(z-R_1e^i n)} - \frac{1}{2} i \frac{1}{z^2(z-R_1e^i p)} \frac{Q}{z} - i \frac{1}{(z-R_1e^i p)} \\ &+ V_o - i \frac{1}{(z-R_1e^i p)} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{2}{z^2(z-R_1e^i p)} \frac{1}{z} - \frac{1}{4} \frac{2}{z^2(z-R_1e^i p)^2} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i p)} \\ &+ \frac{2}{zR_2e^i n} - \frac{1}{2} \frac{2}{z^2(z-R_1e^i p)} \frac{R_1}{zR_1-a^2e^i p} - \frac{1}{4} \frac{2}{z^2(z-R_1e^i n)^2} - \frac{1}{2} i \frac{1}{z^2(zR_1-a^2e^i n)} \\ &+ \frac{Q}{z} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i n)} \frac{1}{z} - i \frac{1}{z^2(zR_1-a^2e^i n)} V_o - i \frac{1}{z^2(zR_1-a^2e^i n)} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i p)} \\ &+ R_2 \frac{2}{zR_2a^2e^i n} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i p)} \frac{2}{zR_2e^i p} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i p)} \frac{2}{zR_2a^2e^i p} - \frac{1}{4} \\ &+ \frac{2}{z^2} - \frac{1}{2} \frac{2}{z^2(zR_1-a^2e^i n)(z-R_1e^i n)} - \frac{1}{4} \frac{2}{z^2(zR_1-a^2e^i n)^2} - \frac{1}{2} \frac{2}{z^2(zR_1-a^2e^i n)(zR_1-a^2e^i p)} - \\ &+ \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i n)} \frac{2}{zR_2e^i n} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i n)} R_2 \frac{2}{zR_2a^2e^i n} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i n)} \frac{2}{zR_2e^i p} - i \\ &+ \frac{1}{(z-R_1e^i n)} V_o - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i n)} \frac{2}{zR_2a^2e^i p} - \frac{1}{2} \frac{2}{z^2(z-R_1e^i n)} \frac{R_1}{zR_1-a^2e^i p} \\ &+ \frac{1}{2} \frac{1}{z^2(z-R_1e^i n)} \frac{2}{zR_2e^i n} - \frac{1}{2} i \frac{1}{z^2(z-R_1e^i n)} \frac{Q}{z} - i \frac{1}{(z-R_1e^i n)} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i n)} \\ &+ \frac{1}{z} - \frac{1}{2} i \frac{1}{z^2(zR_1-a^2e^i p)} \frac{Q}{z} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i p)} \frac{1}{z} - i \frac{1}{z^2(zR_1-a^2e^i p)} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{1}{z^2(z-R_1e^i n)} \\ &+ R_2 \frac{2}{zR_2a^2e^i n} - i \frac{1}{z^2(zR_1-a^2e^i p)} V_o - \frac{1}{2} \frac{1}{z^2(z-R_1e^i n)} \frac{2}{zR_2a^2e^i p} - \\ &+ \frac{1}{2} \frac{1}{z^2(z-R_1e^i n)} \frac{2}{zR_2e^i p} - \frac{1}{2} i \frac{2}{z^2(zR_2e^i n)} \frac{Q}{z} - i \frac{2}{(zR_2e^i n)} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i p)} \\ &+ \frac{2}{zR_2e^i p} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i p)} R_2 \frac{2}{zR_2a^2e^i n} - \frac{1}{4} \frac{2}{z^2(zR_1-a^2e^i p)^2} - \frac{1}{2} \frac{1}{z^2(zR_1-a^2e^i p)} \frac{2}{zR_2e^i n} - \frac{1}{2} \end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{i p})^2} - \frac{R_2}{zR_2 a^2 e^{i p}} - i \frac{2}{(z R_2 e^{i n})} V_o - \frac{1}{2} \frac{2}{(z R_2 e^{i n})^2} \frac{1}{z} - \frac{1}{4} \frac{2}{(z R_2 e^{i n})^2} - \frac{1}{2} \frac{2}{(z R_2 e^{i n})^2} \\
& \frac{R_2}{zR_2 a^2 e^{i p}} - \frac{1}{2} \frac{2}{(z R_2 e^{i n}) (z R_2 e^{i p})} - \frac{1}{2} \frac{2}{(z R_2 e^{i n})} \frac{R_2}{zR_2 a^2 e^{i n}} - \frac{1}{2} i \frac{2}{(z R_2 e^{i p})} \\
& \frac{Q}{z} - i \frac{2}{(z R_2 e^{i p})} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{2}{(z R_2 e^{i p})^2} \frac{1}{z} - \frac{1}{4} \frac{2}{(z R_2 e^{i p})^2} - \frac{1}{4} \frac{2}{(zR_2 a^2 e^{i p})^2} \\
& \frac{1}{2} \frac{2}{(zR_2 a^2 e^{i p}) (z R_2 e^{i p})} - \frac{1}{2} \frac{2}{(zR_2 a^2 e^{i p}) (zR_2 a^2 e^{i n})} - \\
& \frac{1}{2} i \frac{2}{(zR_2 a^2 e^{i p})} \frac{Q}{z} - i \frac{2}{(zR_2 a^2 e^{i p})} V_o - i \frac{2}{(zR_2 a^2 e^{i p})} V_o \frac{a^2}{z^2} - \frac{1}{2} \frac{2}{(zR_2 a^2 e^{i p})} \\
& \frac{1}{z} - \frac{1}{2} \frac{2}{(z R_2 e^{i p})} \frac{R_2}{zR_2 a^2 e^{i n}} - iR_2 \frac{2}{(zR_2 a^2 e^{i n})} V_o - iR_2 \frac{2}{(zR_2 a^2 e^{i n})} \\
& V_o \frac{a^2}{z^2} - \frac{1}{2} R_2 \frac{2}{(zR_2 a^2 e^{i n})} \frac{1}{z} - iV_o \frac{1}{z} - V_o \frac{Q}{z} - \frac{1}{4} R_2^2 \frac{2}{(zR_2 a^2 e^{i n})^2} - \frac{1}{2} iR_2 \frac{2}{(zR_2 a^2 e^{i n})} \frac{Q}{z}
\end{aligned}$$

Para a_1

$$f(z) = V_o^2 \frac{a^4}{z^4}$$

$$Res = \frac{1}{4-1!} \lim_{z \rightarrow 0} \frac{d^{4-1}}{dz^{4-1}} \left(z - 0^{-4} \left(V_o^2 \frac{a^4}{z^4} \right) \right) = 0$$

$$a_1 = 0$$

Para a_2

$$f(z) = -i \frac{2}{(z R_2 e^{i p})} V_o$$

$$a_2 = 0$$

Para a_3

$$f(z) = -\frac{1}{2} i \frac{Q}{z^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^{-2} \left(-\frac{1}{2} i \frac{Q}{z^2} \right) \right) = 0$$

$$a_3 = 0$$

Para a_4

$$f(z) = V_o \frac{a^2}{z^3} \frac{Q}{z}$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0^3 \left(V_o \frac{a^2}{z^3} \right) \right) = 0$$

$$a_4 = 0$$

Para a_5

$$f(z) = -iV_o \frac{a^2}{z^3} -$$

$$\text{Res} = \frac{1}{3-1!} \lim_{z \rightarrow 0} \frac{d^{3-1}}{dz^{3-1}} \left(z - 0^3 \left(-iV_o \frac{a^2}{z^3} - \right) \right) = 0$$

$$a_5 = 0$$

Para a_6

$$f(z) = V_o^2$$

$$a_6 = 0$$

Para a_7

$$f(z) = -2V_o^2 \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^2 \left(-2V_o^2 \frac{a^2}{z^2} \right) \right) = 0$$

$$a_7 = 0$$

Para a_8

$$f(z) = \frac{1}{4} \frac{Q^2}{(z - be^{i ab})^2}$$

$$a_8 = 0$$

Para a_9

$$f(z) = -\frac{1}{2}i \frac{Q}{(z - be^{i ab})^2} R_2 \frac{2}{z R_2 a^2 e^{i n}}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-\frac{1}{2}i \frac{Q}{(z - be^{i ab})^2} R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i n}} \frac{1}{be^{i ab} R_2} \frac{Q}{2} R_2 = 2$$

$$a_9 = \frac{1}{2} \frac{i}{a^2 e^{i n}} \frac{1}{be^{i ab} R_2} \frac{Q}{2} R_2 = 2$$

Para a_{10}

$$f(z) = Q \frac{b}{(zb - a^2 e^{i ab})} V_o$$

$$Res = \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(Q \frac{b}{(zb - a^2 e^{i ab})} V_o \right) \right) = \frac{Q}{2} V_o$$

$$a_{10} = \frac{Q}{2} V_o$$

Para a_{11}

$$f(z) = \frac{1}{2}iQ \frac{b}{(zb - a^2 e^{i ab})^2} \frac{1}{z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(\frac{1}{2}iQ \frac{b}{(zb - a^2 e^{i ab})^2} \frac{1}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i ab}} Q \frac{b}{2}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2}iQ \frac{b}{(zb - a^2 e^{i ab})^2} \frac{1}{z} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i ab}} Q \frac{b}{2}$$

$$a_{11} = Res_1 - Res_2 = 0$$

Para a_{12}

$$f(z) = \frac{1}{4}Q^2 \frac{b^2}{(zb - a^2 e^{i ab})^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right)^2 \left(\frac{1}{4}Q^2 \frac{b^2}{(zb - a^2 e^{i ab})^2} \right) \right) = 0$$

$$a_{12} = 0$$

Para a_{13}

$$f(z) = -\frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} - \frac{2}{zR_2e^{ip}}$$

$$a_{13} = 0$$

Para a_{14}

$$f(z) = -\frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} - \frac{1}{zR_1e^{in}}$$

$$a_{14} = 0$$

Para a_{15}

$$f(z) = -\frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} + \frac{R_1}{zR_1-a^2e^{ip}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2e^{ip}}{R_1}} \left(\left(z - \frac{a^2e^{ip}}{R_1} \right) \left(-\frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} + \frac{R_1}{zR_1-a^2e^{ip}} \right) \right) = \frac{1}{2} \frac{i}{-a^2e^{ip}} \frac{Q}{be^{iab}R_1} - \frac{Q}{2} + R_1$$

$$a_{15} = \frac{1}{2} \frac{i}{-a^2e^{ip}} \frac{Q}{be^{iab}R_1} - \frac{Q}{2} + R_1$$

Para a_{16}

$$f(z) = \frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} + \frac{R_1}{zR_1-a^2e^{in}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2e^{in}}{R_1}} \left(\left(z - \frac{a^2e^{in}}{R_1} \right) \left(\frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} + \frac{R_1}{zR_1-a^2e^{in}} \right) \right) = \frac{1}{2} \frac{i}{a^2e^{in}-be^{iab}R_1} \frac{Q}{2} + R_1$$

$$a_{16} = \frac{1}{2} \frac{i}{a^2e^{in}-be^{iab}R_1} \frac{Q}{2} + R_1$$

Para a_{17}

$$f(z) = \frac{1}{2}i \frac{Q}{z^2(z-be^{iab})} - \frac{2}{zR_2e^{in}}$$

$$a_{17} = 0$$

Para a_{18}

$$f(z) = \frac{1}{2}i \frac{Q}{z^2(z-be^{i\alpha})} \cdot \frac{R_2}{zR_2 - a^2e^{i\alpha}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2e^{i\alpha}}{R_2}} \left(\left(z - \frac{a^2e^{i\alpha}}{R_2} \right) \left(\frac{1}{2}i \frac{Q}{z^2(z-be^{i\alpha})} \cdot \frac{R_2}{zR_2 - a^2e^{i\alpha}} \right) \right) = -\frac{1}{2} \frac{i}{a^2e^{i\alpha}} \frac{Q}{be^{i\alpha}R_2} \cdot \frac{Q}{2} \cdot 2R_2$$

$$a_{18} = -\frac{1}{2} \frac{i}{a^2e^{i\alpha}} \frac{Q}{be^{i\alpha}R_2} \cdot \frac{Q}{2} \cdot 2R_2$$

Para a_{19}

$$f(z) = \frac{1}{2} \frac{Q^2}{z^2(z-be^{i\alpha})} \cdot \frac{b}{zb-a^2e^{i\alpha}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2e^{i\alpha}}{b}} \left(\left(z - \frac{a^2e^{i\alpha}}{b} \right) \left(\frac{1}{2} \frac{Q^2}{z^2(z-be^{i\alpha})} \cdot \frac{b}{zb-a^2e^{i\alpha}} \right) \right) = -\frac{1}{2e^{i\alpha}} \frac{1}{ab-a^2} \cdot \frac{Q^2}{b^2} b$$

$$a_{19} = -\frac{1}{2e^{i\alpha}} \frac{1}{ab-a^2} \cdot \frac{Q^2}{b^2} b$$

Para a_{20}

$$f(z) = -\frac{1}{2} \frac{Q^2}{z^2(z-be^{i\alpha})z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} \frac{Q^2}{z^2(z-be^{i\alpha})z} \right) \right) = \frac{1}{2be^{i\alpha}} \cdot \frac{Q^2}{2}$$

$$a_{20} = \frac{1}{2be^{i\alpha}} \cdot \frac{Q^2}{2}$$

Para a_{21}

$$f(z) = \frac{1}{2}i \frac{Q}{z^2(z-be^{i\alpha})} \cdot \frac{1}{z-R_1e^{i\alpha}}$$

$$a_{21} = 0$$

Para a_{22}

$$f(z) = \frac{Q}{(z - be^{i ab})} V_o$$

$$a_{22} = 0$$

Para a_{23}

$$f(z) = -\frac{Q}{(z - be^{i ab})} V_o \frac{a^2}{z^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-\frac{Q}{(z - be^{i ab})} V_o \frac{a^2}{z^2} \right) = \frac{1}{b^2 e^{2i ab}} Q V_o \frac{a^2}{z^2}$$

$$a_{23} = \frac{1}{b^2 e^{2i ab}} Q V_o \frac{a^2}{z^2}$$

Para a_{24}

$$f(z) = \frac{1}{2} i \frac{Q}{z^2 (z - be^{i ab})} \frac{1}{z}$$

$$Res = \lim_{z \rightarrow 0} z \left(z - 0 \right) \left(\frac{1}{2} i \frac{Q}{z^2 (z - be^{i ab})} \frac{1}{z} \right) = -\frac{1}{2} \frac{i}{be^{i ab}} \frac{Q}{z^2}$$

$$a_{24} = -\frac{1}{2} \frac{i}{be^{i ab}} \frac{Q}{z^2}$$

Para a_{25}

$$f(z) = \frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} + \frac{R_1}{z R_1 - a^2 e^{i n}}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} + \frac{R_1}{z R_1 - a^2 e^{i n}} \right) \right)$$

$$= -\frac{1}{2} \frac{i}{a^2 (-e^{i ab} R_1 - e^{i n} b)} Q \frac{b}{z^2} + R_1$$

$$Res_2 = \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} + \frac{R_1}{z R_1 - a^2 e^{i n}} \right) \right)$$

$$= \frac{1}{2} \frac{i}{a^2 (-e^{i ab} R_1 - e^{i n} b)} Q \frac{b}{z^2} + R_1$$

$$a_{25} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{26}

$$f(z) = -\frac{1}{2}iQ \frac{b}{z^2(zb-a^2e^{iab})} + \frac{R_1}{zR_1-a^2e^{ip}}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2e^{iab}}{b}} \left(\left(z - \frac{a^2e^{iab}}{b} \right) \left(-\frac{1}{2}iQ \frac{b}{z^2(zb-a^2e^{iab})} + \frac{R_1}{zR_1-a^2e^{ip}} \right) \right)$$

$$= -\frac{1}{2} \frac{i}{a^2(e^{iab}R_1-e^{ip}b)} Q \frac{b}{z} + R_1$$

$$Res_2 = \lim_{z \rightarrow \frac{a^2e^{ip}}{R_1}} \left(\left(z - \frac{a^2e^{ip}}{R_1} \right) \left(-\frac{1}{2}iQ \frac{b}{z^2(zb-a^2e^{iab})} + \frac{R_1}{zR_1-a^2e^{ip}} \right) \right)$$

$$= \frac{1}{2} \frac{i}{a^2(e^{iab}R_1-e^{ip}b)} Q \frac{b}{z} + R_1$$

$$a_{26} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{27}

$$f(z) = \frac{1}{2}iQ \frac{b}{z^2(zb-a^2e^{iab})} + \frac{2}{zR_2e^{in}}$$

$$Res = \lim_{z \rightarrow \frac{a^2e^{iab}}{b}} \left(\left(z - \frac{a^2e^{iab}}{b} \right) \left(\frac{1}{2}iQ \frac{b}{z^2(zb-a^2e^{iab})} + \frac{2}{zR_2e^{in}} \right) \right) = \frac{1}{2} \frac{i}{a^2e^{iab}R_2e^{in}b} Q \frac{b}{z} + 2$$

$$a_{27} = \frac{1}{2} \frac{i}{a^2e^{iab}R_2e^{in}b} Q \frac{b}{z} + 2$$

Para a_{28}

$$f(z) = -\frac{1}{2}Q^2 \frac{b}{z^2(zb-a^2e^{iab})z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2e^{iab}}{b}} \left(\left(z - \frac{a^2e^{iab}}{b} \right) \left(-\frac{1}{2}Q^2 \frac{b}{z^2(zb-a^2e^{iab})z} \right) \right) = -\frac{1}{2a^2e^{iab}} Q^2 \frac{b}{z}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2}Q^2 \frac{b}{z^2(zb-a^2e^{iab})z} \right) \right) = \frac{1}{2a^2e^{iab}} Q^2 \frac{b}{z}$$

$$a_{28} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{29}

$$f(z) = \frac{1}{2} iQ \frac{b}{(zb - a^2 e^{i ab})} \frac{1}{z - R_1 e^{i p}}$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(\frac{1}{2} iQ \frac{b}{(zb - a^2 e^{i ab})} \frac{1}{z - R_1 e^{i p}} \right) \right) = -\frac{1}{2} \frac{i}{-a^2 e^{i ab} R_1 e^{i p} b} Q \frac{b}{2} \quad 1$$

$$a_{29} = -\frac{1}{2} \frac{i}{-a^2 e^{i ab} R_1 e^{i p} b} Q \frac{b}{2} \quad 1$$

Para a_{30}

$$f(z) = -Q \frac{b}{(zb - a^2 e^{i ab})} V_o \frac{a^2}{z^2}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(-Q \frac{b}{(zb - a^2 e^{i ab})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{b^2}{a^2 e^{2i ab}} \frac{Q}{V_o}$$

$$Res_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-Q \frac{b}{(zb - a^2 e^{i ab})} V_o \frac{a^2}{z^2} \right) = \frac{b^2}{a^2 e^{2i ab}} \frac{Q}{V_o}$$

$$a_{30} = Res_1 + Res_2 = 0$$

Para a_{31}

$$f(z) = -\frac{1}{2} iQ \frac{b}{(zb - a^2 e^{i ab})} \frac{1}{z - R_1 e^{i n}}$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(-\frac{1}{2} iQ \frac{b}{(zb - a^2 e^{i ab})} \frac{1}{z - R_1 e^{i n}} \right) \right) = \frac{1}{2} \frac{i}{-a^2 e^{i ab} R_1 e^{i n} b} Q \frac{b}{2} \quad 1$$

$$a_{31} = \frac{1}{2} \frac{i}{-a^2 e^{i ab} R_1 e^{i n} b} Q \frac{b}{2} \quad 1$$

Para a_{32}

$$f(z) = \frac{1}{2} iQ \frac{b}{(zb - a^2 e^{i ab})} \frac{R_2}{z R_2 a^2 e^{i p}}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - \frac{R_2}{z R_2 a^2 e^{i p}} \right) \right)$$

$$- \frac{1}{2} \frac{i}{a^2 (R_2 e^{i ab} e^{i pb})} Q \frac{b}{2} - 2 R_2$$

$$Res_2 \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - \frac{R_2}{z R_2 a^2 e^{i p}} \right) \right)$$

$$- \frac{1}{2} \frac{i}{a^2 (R_2 e^{i ab} e^{i pb})} Q \frac{b}{2} - 2 R_2$$

$$a_{32} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{33}

$$f(z) = -\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - \frac{2}{z R_2 e^{i p}}$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(-\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - \frac{2}{z R_2 e^{i p}} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i ab} R_2 e^{i pb}} Q \frac{b}{2} - 2$$

$$a_{33} = -\frac{1}{2} \frac{i}{a^2 e^{i ab} R_2 e^{i pb}} Q \frac{b}{2} - 2$$

Para a_{34}

$$f(z) = -\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - R_2 \frac{2}{z R_2 a^2 e^{i n}}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i ab}}{b}} \left(\left(z - \frac{a^2 e^{i ab}}{b} \right) \left(-\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right)$$

$$- \frac{1}{2} \frac{i}{a^2 (R_2 e^{i ab} e^{i nb})} Q \frac{b}{2} - 2 R_2$$

$$Res_2 \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-\frac{1}{2} i Q \frac{b}{z^2 (zb - a^2 e^{i ab})} - R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right)$$

$$\frac{1}{2} \frac{i}{a^2 (R_2 e^{i ab} e^{i nb})} Q \frac{b}{2} - 2 R_2$$

$$a_{34} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{35}

$$f(z) = \frac{1}{4} \frac{Q^2}{z^2}$$

$$\text{Res} \quad \frac{1}{2-1} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0^2 \left(\frac{1}{4} \frac{Q^2}{2z^2} \right) \right) = 0$$

$$a_{35} = 0$$

Para a_{36}

$$f(z) = -\frac{1}{2} \frac{i}{z^2(z-R_1 e^{i p})} \frac{R_1}{z R_1 - a^2 e^{i n}}$$

$$\text{Res} \quad \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(-\frac{1}{2} \frac{i}{z^2(z-R_1 e^{i p})} \frac{R_1}{z R_1 - a^2 e^{i n}} \right) \right) = \frac{1}{2(-a^2 e^{i n} - e^{i p} R_1^2)} - \frac{i}{2} R_1$$

$$a_{36} = \frac{1}{2(-a^2 e^{i n} - e^{i p} R_1^2)} - \frac{i}{2} R_1$$

Para a_{37}

$$f(z) = \frac{1}{2} \frac{i}{z^2(z-R_1 e^{i p})(z-R_1 e^{i n})}$$

$$a_{37} = 0$$

Para a_{38}

$$f(z) = -\frac{1}{2} i \frac{1}{z^2(z-R_1 e^{i p})} \frac{Q}{z}$$

$$\text{Res} \quad \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} i \frac{1}{z^2(z-R_1 e^{i p})} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{R_1 e^{i p}} - \frac{1}{2} Q$$

$$a_{38} = \frac{1}{2} \frac{i}{R_1 e^{i p}} - \frac{1}{2} Q$$

Para a_{39}

$$f(z) = i \frac{1}{(z-R_1 e^{i p})} V_o$$

$$a_{39} = 0$$

Para a_{40}

$$f(z) = -i \frac{1}{(z - R_1 e^{i p})} V_o \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-i \frac{1}{(z - R_1 e^{i p})} V_o \frac{a^2}{z^2} \right) = \frac{i}{R_1^2 e^{2 i p}} V_o a^2$$

$$a_{40} = \frac{i}{R_1^2 e^{2 i p}} V_o a^2$$

Para a_{41}

$$f(z) = -\frac{1}{2} \frac{1}{(z - R_1 e^{i p})} \frac{1}{z}$$

$$\text{Res} = \lim_{z \rightarrow 0} \left(z - 0 \right) \left(-\frac{1}{2} \frac{1}{(z - R_1 e^{i p})} \frac{1}{z} \right) = \frac{1}{2 R_1 e^{i p}} - \frac{1}{2}$$

$$a_{41} = \frac{1}{2 R_1 e^{i p}} - \frac{1}{2}$$

Para a_{42}

$$f(z) = -\frac{1}{4} \frac{1}{(z - R_1 e^{i p})^2}$$

$$a_{42} = 0$$

Para a_{43}

$$f(z) = -\frac{1}{2} \frac{1}{(z - R_1 e^{i p})} \frac{2}{z R_2 e^{i n}}$$

$$a_{43} = 0$$

Para a_{44}

$$f(z) = \frac{1}{2} \frac{1}{(z - R_1 e^{i p})} \frac{R_1}{z R_1 - a^2 e^{i p}}$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(\frac{1}{2} \frac{1}{z - R_1 e^{i p}} \frac{R_1}{z R_1 - a^2 e^{i p}} \right) \right) = -\frac{1}{2 e^{i p} (-a^2 R_1^2)} \frac{1}{2} R_1$$

$$a_{44} = -\frac{1}{2 e^{i p} (-a^2 R_1^2)} \frac{1}{2} R_1$$

Para a_{45}

$$f(z) = -\frac{1}{4} \frac{1}{z^2 (z - R_1 e^{i n})^2}$$

$$a_{45} = 0$$

Para a_{46}

$$f(z) = -\frac{1}{2} i \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{Q}{z}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(-\frac{1}{2} i \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i n}} \frac{1}{z} \frac{R_1}{2} Q$$

$$Res_2 \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} i \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i n}} \frac{1}{z} \frac{R_1}{2} Q$$

$$a_{46} = Res_1 + Res_2 = 0$$

Para a_{47}

$$f(z) = -\frac{1}{2} \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{1}{z}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(-\frac{1}{2} \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{1}{z} \right) \right) = -\frac{1}{2 a^2 e^{i n}} \frac{1}{z} \frac{R_1}{2}$$

$$Res_2 \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} \frac{1}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} \frac{1}{z} \right) \right) = \frac{1}{2 a^2 e^{i n}} \frac{1}{z} \frac{R_1}{2}$$

$$a_{47} = Res_1 + Res_2 = 0$$

Para a_{48}

$$f(z) = i \frac{1}{z} \frac{R_1}{(zR_1 - a^2 e^{i n})} V_o$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(i \frac{1}{z} \frac{R_1}{(zR_1 - a^2 e^{i n})} V_o \right) \right) = i \frac{1}{z} V_o$$

$$a_{48} = i \frac{1}{z} V_o$$

Para a_{49}

$$f(z) = -i \frac{1}{z} \frac{R_1}{(zR_1 - a^2 e^{i n})} V_o \frac{a^2}{z^2}$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(-i \frac{1}{z} \frac{R_1}{(zR_1 - a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = -i \frac{R_1^2}{a^2 e^{2 i n}} \frac{1}{z} V_o$$

$$Res_2 = \frac{1}{2(-1)!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-i \frac{1}{z} \frac{R_1}{(zR_1 - a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) = i \frac{R_1^2}{a^2 e^{2 i n}} \frac{1}{z} V_o$$

$$a_{49} = Res_1 + Res_2 = 0$$

Para a_{50}

$$f(z) = \frac{1}{2} \frac{1}{z^2 (z - R_1 e^{i p})} R_2 \frac{2}{z R_2 a^2 e^{i n}}$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(\frac{1}{2} \frac{1}{z^2 (z - R_1 e^{i p})} R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right) = - \frac{1}{2(a^2 e^{i n} - R_1 e^{i p} R_2)} \frac{1}{z} R_2$$

$$a_{50} = - \frac{1}{2(a^2 e^{i n} - R_1 e^{i p} R_2)} \frac{1}{z} R_2$$

Para a_{51}

$$f(z) = \frac{1}{2} \frac{1}{z^2 (z - R_1 e^{i p})} \frac{2}{z R_2 e^{i p}}$$

$$a_{51} = 0$$

Para a_{52}

$$f(z) = -\frac{1}{2} \frac{1}{z - R_1 e^{i p}} + \frac{R_2}{z R_2 - a^2 e^{i p}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-\frac{1}{2} \frac{1}{z - R_1 e^{i p}} + \frac{R_2}{z R_2 - a^2 e^{i p}} \right) \right) = \frac{1}{2(a^2 e^{i p} - R_1 e^{i p} R_2)} - \frac{1}{2} R_2$$

$$a_{52} = \frac{1}{2(a^2 e^{i p} - R_1 e^{i p} R_2)} - \frac{1}{2} R_2$$

Para a_{53}

$$f(z) = -\frac{1}{4} \frac{2}{z^2}$$

$$\text{Res} \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \right)^2 \left(-\frac{1}{4} \frac{2}{z^2} \right) = 0$$

$$a_{53} = 0$$

Para a_{54}

$$f(z) = \frac{1}{2} \frac{2}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} (z - R_1 e^{i n})$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(\frac{1}{2} \frac{2}{z} \frac{R_1}{z R_1 - a^2 e^{i n}} (z - R_1 e^{i n}) \right) \right) = -\frac{1}{2 e^{i n} (-a^2 - R_1^2)} - \frac{2}{1} \frac{R_1}{2}$$

$$a_{54} = -\frac{1}{2 e^{i n} (-a^2 - R_1^2)} - \frac{2}{1} \frac{R_1}{2}$$

Para a_{55}

$$f(z) = -\frac{1}{4} \frac{2}{z} \frac{R_1^2}{z R_1 - a^2 e^{i n}} (z - R_1 e^{i n})^2$$

$$\text{Res} \frac{1}{2-1!} \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right)^2 \left(-\frac{1}{4} \frac{2}{z} \frac{R_1^2}{z R_1 - a^2 e^{i n}} (z - R_1 e^{i n})^2 \right) \right) = 0$$

$$a_{55} = 0$$

Para a_{56}

$$f(z) = \frac{1}{2} \frac{R_1^2}{(zR_1 - a^2 e^{in})(zR_1 - a^2 e^{ip})}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{in}}{R_1}} \left(\left(z - \frac{a^2 e^{in}}{R_1} \right) \left(\frac{1}{2} \frac{R_1^2}{(zR_1 - a^2 e^{in})(zR_1 - a^2 e^{ip})} \right) \right) = \frac{1}{2} \frac{R_1}{a^2 (e^{in} - e^{ip})} \frac{1}{2}$$

$$Res_2 = \lim_{z \rightarrow \frac{a^2 e^{ip}}{R_1}} \left(\left(z - \frac{a^2 e^{ip}}{R_1} \right) \left(\frac{1}{2} \frac{R_1^2}{(zR_1 - a^2 e^{in})(zR_1 - a^2 e^{ip})} \right) \right) = -\frac{1}{2} \frac{R_1}{a^2 (e^{in} - e^{ip})} \frac{1}{2}$$

$$a_{56} = Res_1 - Res_2 = 0$$

Para a_{57}

$$f(z) = -\frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{in})} \frac{2}{zR_2 e^{in}}$$

$$Res = \lim_{z \rightarrow \frac{a^2 e^{in}}{R_1}} \left(\left(z - \frac{a^2 e^{in}}{R_1} \right) \left(-\frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{in})} \frac{2}{zR_2 e^{in}} \right) \right) = -\frac{1}{2(a^2 e^{in} R_2 e^{in} R_1)} \frac{R_1}{2} = 2$$

$$a_{57} = -\frac{1}{2(a^2 e^{in} R_2 e^{in} R_1)} \frac{R_1}{2} = 2$$

Para a_{58}

$$f(z) = \frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{in})} R_2 \frac{2}{zR_2 a^2 e^{in}}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{in}}{R_1}} \left(\left(z - \frac{a^2 e^{in}}{R_1} \right) \left(\frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{in})} R_2 \frac{2}{zR_2 a^2 e^{in}} \right) \right)$$

$$= \frac{1}{2a^2 (e^{in} R_1 e^{in} R_2)} \frac{R_1}{2} = 2R_2$$

$$Res_2 = \lim_{z \rightarrow -\frac{a^2 e^{in}}{R_2}} \left(\left(z - \frac{a^2 e^{in}}{R_2} \right) \left(\frac{1}{2} \frac{R_1}{(zR_1 - a^2 e^{in})} R_2 \frac{2}{zR_2 a^2 e^{in}} \right) \right)$$

$$= -\frac{1}{2a^2 (e^{in} R_1 e^{in} R_2)} \frac{R_1}{2} = 2R_2$$

$$a_{58} = Res_1 - Res_2 = 0$$

Para a_{59}

$$f(z) = \frac{1}{2} \left(1 - \frac{R_1}{zR_1 - a^2 e^{i n}} - \frac{2}{zR_2 e^{i p}} \right)$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(\frac{1}{2} \left(1 - \frac{R_1}{zR_1 - a^2 e^{i n}} - \frac{2}{zR_2 e^{i p}} \right) \right) \right) = \frac{1}{2(a^2 e^{i n} - R_2 e^{i p} R_1)} \left(1 - \frac{R_1}{2} \right)$$

$$a_{59} = \frac{1}{2(a^2 e^{i n} - R_2 e^{i p} R_1)} \left(1 - \frac{R_1}{2} \right)$$

Para a_{60}

$$f(z) = -i \frac{1}{(z - R_1 e^{i n})} V_o$$

$$a_{60} = 0$$

Para a_{61}

$$f(z) = -\frac{1}{2} \left(1 - \frac{R_1}{zR_1 - a^2 e^{i n}} - 2 \frac{R_2}{zR_2 - a^2 e^{i p}} \right)$$

$$Res_1 \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_1}} \left(\left(z - \frac{a^2 e^{i n}}{R_1} \right) \left(-\frac{1}{2} \left(1 - \frac{R_1}{zR_1 - a^2 e^{i n}} - 2 \frac{R_2}{zR_2 - a^2 e^{i p}} \right) \right) \right) = -\frac{1}{2a^2(e^{i n} R_2 - e^{i p} R_1)} \left(1 - \frac{R_1}{2} - 2R_2 \right)$$

$$Res_2 \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-\frac{1}{2} \left(1 - \frac{R_1}{zR_1 - a^2 e^{i n}} - 2 \frac{R_2}{zR_2 - a^2 e^{i p}} \right) \right) \right) = \frac{1}{2a^2(e^{i n} R_2 - e^{i p} R_1)} \left(1 - \frac{R_1}{2} - 2R_2 \right)$$

$$a_{61} = Res_1 + Res_2 = 0$$

Para a_{62}

$$f(z) = -\frac{1}{2} \left(\frac{1}{z - R_1 e^{i n}} - \frac{R_1}{zR_1 - a^2 e^{i p}} \right)$$

$$Res \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(-\frac{1}{2} \left(\frac{1}{z - R_1 e^{i n}} - \frac{R_1}{zR_1 - a^2 e^{i p}} \right) \right) \right) = -\frac{1}{2(a^2 e^{i p} - R_1^2 e^{i n})} - \frac{1}{2} R_1$$

$$a_{62} = -\frac{1}{2(a^2 e^{i p} - R_1^2 e^{i n})} - \frac{1}{2} R_1$$

Para a_{63}

$$f(z) = \frac{1}{2} \frac{1}{(z - R_1 e^{i n})} \frac{2}{z R_2 e^{i n}}$$

$$a_{63} = 0$$

Para a_{64}

$$f(z) = \frac{1}{2} i \frac{1}{(z - R_1 e^{i n})} \frac{Q}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i \frac{1}{(z - R_1 e^{i n})} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{R_1 e^{i n}} \frac{1}{2} Q$$

$$a_{64} = -\frac{1}{2} \frac{i}{R_1 e^{i n}} \frac{1}{2} Q$$

Para a_{65}

$$f(z) = i \frac{1}{(z - R_1 e^{i n})} V_o \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(i \frac{1}{(z - R_1 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{i}{R_1^2 e^{2i n}} V_o a^2$$

$$a_{65} = -\frac{i}{R_1^2 e^{2i n}} V_o a^2$$

Para a_{66}

$$f(z) = \frac{1}{2} \frac{1}{(z - R_1 e^{i n})} \frac{1}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} \frac{1}{(z - R_1 e^{i n})} \frac{1}{z} \right) \right) = -\frac{1}{2 R_1 e^{i n}} \frac{1}{2}$$

$$a_{66} = -\frac{1}{2 R_1 e^{i n}} \frac{1}{2}$$

Para a_{67}

$$f(z) = \frac{1}{2} i \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{Q}{z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(\frac{1}{2} i \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i p}} \frac{1}{1 - \frac{R_1}{2}} Q$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i p}} \frac{1}{1 - \frac{R_1}{2}} Q$$

$$a_{67} \quad Res_1 - Res_2 = 0$$

Para a_{68}

$$f(z) = \frac{1}{2} \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{1}{z}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(\frac{1}{2} \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{1}{z} \right) \right) = \frac{1}{2a^2 e^{i p}} \frac{1}{1 - \frac{R_1}{2}}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} \frac{1}{1 - \frac{R_1}{2(zR_1 - a^2 e^{i p})}} \frac{1}{z} \right) \right) = -\frac{1}{2a^2 e^{i p}} \frac{1}{1 - \frac{R_1}{2}}$$

$$a_{68} \quad Res_1 - Res_2 = 0$$

Para a_{69}

$$f(z) = i \frac{1}{1 - \frac{R_1}{(zR_1 - a^2 e^{i p})}} V_o \frac{a^2}{z^2}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(i \frac{1}{1 - \frac{R_1}{(zR_1 - a^2 e^{i p})}} V_o \frac{a^2}{z^2} \right) \right) = \frac{i}{a^2 e^{2 i p}} \frac{1}{1 - \frac{R_1}{2}} V_o$$

$$Res_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(i \frac{1}{1 - \frac{R_1}{(zR_1 - a^2 e^{i p})}} V_o \frac{a^2}{z^2} \right) \right) = -\frac{i}{a^2 e^{2 i p}} \frac{1}{1 - \frac{R_1}{2}} V_o$$

$$a_{69} \quad Res_1 - Res_2 = 0$$

Para a_{70}

$$f(z) = -\frac{1}{2} \frac{1}{1 - \frac{1}{2(z - R_1 e^{i n})}} R_2 \frac{2}{z R_2 a^2 e^{i n}}$$

$$\text{Res} \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-\frac{1}{2} \frac{1}{z - R_1 e^{i n}} R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right) = \frac{1}{2(a^2 e^{i n} R_1 e^{i n} R_2)} \frac{1}{2} 2R_2$$

$$a_{70} = \frac{1}{2(a^2 e^{i n} R_1 e^{i n} R_2)} \frac{1}{2} 2R_2$$

Para a_{71}

$$f(z) = -i \frac{1}{z - R_1 a^2 e^{i p}} V_o$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(-i \frac{1}{z - R_1 a^2 e^{i p}} V_o \right) \right) = -i \frac{1}{R_1} V_o$$

$$a_{71} = -i \frac{1}{R_1} V_o$$

Para a_{72}

$$f(z) = \frac{1}{2} \frac{1}{z - R_1 e^{i n}} \frac{2}{z R_2 a^2 e^{i p}} R_2$$

$$\text{Res} \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(\frac{1}{2} \frac{1}{z - R_1 e^{i n}} \frac{2}{z R_2 a^2 e^{i p}} R_2 \right) \right) = -\frac{1}{2(a^2 e^{i p} R_1 e^{i n} R_2)} \frac{1}{2} 2R_2$$

$$a_{72} = -\frac{1}{2(a^2 e^{i p} R_1 e^{i n} R_2)} \frac{1}{2} 2R_2$$

Para a_{73}

$$f(z) = -\frac{1}{2} \frac{1}{z - R_1 e^{i n}} \frac{2}{z R_2 e^{i p}}$$

$$a_{73} = 0$$

Para a_{74}

$$f(z) = -\frac{1}{2} i \frac{2}{z R_2 e^{i n}} \frac{Q}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} i \frac{2}{z R_2 e^{i n}} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{R_2 e^{i n}} \frac{2}{2} Q$$

$$a_{74} = -\frac{1}{2} \frac{i}{R_2 e^{i n}} \frac{2}{2} Q$$

Para a_{75}

$$f(z) = -i \frac{2}{(z R_2 e^{i n})} V_o \frac{a^2}{z^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left((z-0)^2 \left(-i \frac{2}{(z R_2 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = \frac{i}{R_2^2 e^{2 i n}} 2 V_o a^2$$

$$a_{75} = \frac{i}{R_2^2 e^{2 i n}} 2 V_o a^2$$

Para a_{76}

$$f(z) = -\frac{1}{2} \frac{1}{z^2} \frac{R_1}{(z R_1 - a^2 e^{i p})} \frac{2}{z R_2 e^{i p}}$$

$$Res = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(-\frac{1}{2} \frac{1}{z^2} \frac{R_1}{(z R_1 - a^2 e^{i p})} \frac{2}{z R_2 e^{i p}} \right) \right) = -\frac{1}{2(a^2 e^{i p} R_2 e^{i p} R_1)} \frac{1}{2} R_1$$

$$a_{76} = -\frac{1}{2(a^2 e^{i p} R_2 e^{i p} R_1)} \frac{1}{2} R_1$$

Para a_{77}

$$f(z) = -\frac{1}{2} \frac{1}{z^2} \frac{R_1}{(z R_1 - a^2 e^{i p})} R_2 \frac{2}{z R_2 a^2 e^{i n}}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(-\frac{1}{2} \frac{1}{z^2} \frac{R_1}{(z R_1 - a^2 e^{i p})} R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right)$$

$$= -\frac{1}{2a^2 (e^{i n} R_1 e^{i p} R_2)} \frac{1}{2} R_1 R_2$$

$$Res_2 = \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-\frac{1}{2} \frac{1}{z^2} \frac{R_1}{(z R_1 - a^2 e^{i p})} R_2 \frac{2}{z R_2 a^2 e^{i n}} \right) \right)$$

$$= \frac{1}{2a^2 (e^{i n} R_1 e^{i p} R_2)} \frac{1}{2} R_1 R_2$$

$$a_{77} = Res_1 + Res_2 = 0$$

Para a_{78}

$$f(z) = -\frac{1}{4} \frac{2}{1} \frac{R_1^2}{(zR_1 - a^2 e^{i p})^2}$$

$$\text{Res} = \frac{1}{2-1} \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right)^2 \left(-\frac{1}{4} \frac{2}{1} \frac{R_1^2}{(zR_1 - a^2 e^{i p})^2} \right) \right) = 0$$

$$a_{78} = 0$$

Para a_{79}

$$f(z) = \frac{1}{2} \frac{1}{1} \frac{R_1}{(zR_1 - a^2 e^{i p})} \frac{2}{z R_2 e^{i n}}$$

$$\text{Res} = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(\frac{1}{2} \frac{1}{1} \frac{R_1}{(zR_1 - a^2 e^{i p})} \frac{2}{z R_2 e^{i n}} \right) \right) = \frac{1}{2(a^2 e^{i p} R_2 e^{i n} R_1)} \frac{1}{1} \frac{R_1}{2}$$

$$a_{79} = \frac{1}{2(a^2 e^{i p} R_2 e^{i n} R_1)} \frac{1}{1} \frac{R_1}{2}$$

Para a_{80}

$$f(z) = \frac{1}{2} \frac{1}{1} \frac{R_1}{(zR_1 - a^2 e^{i p})} \frac{2}{z R_2} \frac{R_2}{a^2 e^{i p}}$$

$$\text{Res}_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_1}} \left(\left(z - \frac{a^2 e^{i p}}{R_1} \right) \left(\frac{1}{2} \frac{1}{1} \frac{R_1}{(zR_1 - a^2 e^{i p})} \frac{2}{z R_2} \frac{R_2}{a^2 e^{i p}} \right) \right)$$

$$= \frac{1}{2a^2 (e^{i p} R_2 e^{i p} R_1)} \frac{1}{1} \frac{R_1}{2} \frac{2}{R_2}$$

$$\text{Res}_2 = \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(\frac{1}{2} \frac{1}{1} \frac{R_1}{(zR_1 - a^2 e^{i p})} \frac{2}{z R_2} \frac{R_2}{a^2 e^{i p}} \right) \right)$$

$$= -\frac{1}{2a^2 (e^{i p} R_2 e^{i p} R_1)} \frac{1}{1} \frac{R_1}{2} \frac{2}{R_2}$$

$$a_{80} = \text{Res}_1 - \text{Res}_2 = 0$$

Para a_{81}

$$f(z) = i \frac{2}{(z R_2 e^{i n})} V_o$$

$$a_{81} = 0$$

Para a_{82}

$$f(z) = -\frac{1}{2} \frac{z^2}{z^2 (z - R_2 e^{i n})} \frac{1}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} \frac{z^2}{z^2 (z - R_2 e^{i n})} \frac{1}{z} \right) \right) = -\frac{1}{2 R_2 e^{i n}} \frac{1}{2}$$

$$a_{82} = -\frac{1}{2 R_2 e^{i n}} \frac{1}{2}$$

Para a_{83}

$$f(z) = -\frac{1}{4} \frac{z^{\frac{3}{2}}}{z^2 (z - R_2 e^{i n})^2}$$

$$a_{83} = 0$$

Para a_{84}

$$f(z) = -\frac{1}{2} \frac{z^{\frac{3}{2}}}{z^2 (z - R_2 e^{i n})} \frac{R_2}{z R_2 a^2 e^{i p}}$$

$$\text{Res} \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-\frac{1}{2} \frac{z^{\frac{3}{2}}}{z^2 (z - R_2 e^{i n})} \frac{R_2}{z R_2 a^2 e^{i p}} \right) \right) = \frac{1}{2 (a^2 e^{i p} - e^{i n} R_2^2)} \frac{1}{2} R_2$$

$$a_{84} = \frac{1}{2 (a^2 e^{i p} - e^{i n} R_2^2)} \frac{1}{2} R_2$$

Para a_{85}

$$f(z) = \frac{1}{2} \frac{z^{\frac{3}{2}}}{z^2 (z - R_2 e^{i n}) (z - R_2 e^{i p})}$$

$$a_{85} = 0$$

Para a_{86}

$$f(z) = \frac{1}{2} \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i n})} \frac{R_2}{z R_2 a^2 e^{i n}}$$

$$\text{Res} \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(\frac{1}{2} \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i n})} \frac{R_2}{z R_2 a^2 e^{i n}} \right) \right) = \frac{1}{2 e^{i n} (-a^2 R_2^2)} \frac{\frac{2}{2}}{2} R_2$$

$$a_{86} = \frac{1}{2 e^{i n} (-a^2 R_2^2)} \frac{\frac{2}{2}}{2} R_2$$

Para a_{87}

$$f(z) = \frac{1}{2} i \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i p})} \frac{Q}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i p})} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{R_2 e^{i p}} \frac{\frac{2}{2}}{2} Q$$

$$a_{87} = \frac{1}{2} \frac{i}{R_2 e^{i p}} \frac{\frac{2}{2}}{2} Q$$

Para a_{88}

$$f(z) = i \frac{z^{\frac{2}{2}}}{(z R_2 e^{i p})} V_o \frac{a^2}{z^2}$$

$$\text{Res} = \frac{1}{2-1} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(i \frac{z^{\frac{2}{2}}}{(z R_2 e^{i p})} V_o \frac{a^2}{z^2} \right) \right) = - \frac{i}{R_2^2 e^{2 i p}} 2 V_o a^2$$

$$a_{88} = - \frac{i}{R_2^2 e^{2 i p}} 2 V_o a^2$$

Para a_{89}

$$f(z) = \frac{1}{2} \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i p})} \frac{1}{z}$$

$$\text{Res} \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} \frac{z^{\frac{2}{2}}}{z^2 (z R_2 e^{i p})} \frac{1}{z} \right) \right) = \frac{1}{2 R_2 e^{i p}} \frac{\frac{2}{2}}{2}$$

$$a_{89} = \frac{1}{2 R_2 e^{i p}} \frac{\frac{2}{2}}{2}$$

Para a_{90}

$$f(z) = -\frac{1}{4} \frac{z^{\frac{2}{2}}}{(z - R_2 e^{i p})^2}$$

$$a_{90} = 0$$

Para a_{91}

$$f(z) = -\frac{1}{4} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_2}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right)^2 \left(-\frac{1}{4} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})^2} \right) \right) = 0$$

$$a_{91} = 0$$

Para a_{92}

$$f(z) = \frac{1}{2} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})(z - R_2 e^{i p})}$$

$$Res = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(\frac{1}{2} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})(z - R_2 e^{i p})} \right) \right) = \frac{1}{2 e^{i p} (-a^2 - R_2^2)} R_2 \frac{z^{\frac{2}{2}}}{2}$$

$$a_{92} = \frac{1}{2 e^{i p} (-a^2 - R_2^2)} R_2 \frac{z^{\frac{2}{2}}}{2}$$

Para a_{93}

$$f(z) = \frac{1}{2} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})(z - R_2 a^2 e^{i n})}$$

$$Res_1 = \lim_{z \rightarrow \frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(\frac{1}{2} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})(z - R_2 a^2 e^{i n})} \right) \right) = \frac{1}{2} \frac{R_2}{a^2 (-e^{i p} - e^{i n})} \frac{z^{\frac{2}{2}}}{2}$$

$$Res_2 = \lim_{z \rightarrow \frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(\frac{1}{2} \frac{z^{\frac{2}{2}}}{(z - R_2 a^2 e^{i p})(z - R_2 a^2 e^{i n})} \right) \right) = -\frac{1}{2} \frac{R_2}{a^2 (-e^{i p} - e^{i n})} \frac{z^{\frac{2}{2}}}{2}$$

$$a_{93} = Res_1 - Res_2 = 0$$

Para a_{94}

$$f(z) = -\frac{1}{2} i \frac{R_2}{z^2 (zR_2 - a^2 e^{i p})} \frac{Q}{z}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-\frac{1}{2} i \frac{R_2}{z^2 (zR_2 - a^2 e^{i p})} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i p}} \frac{R_2}{z^2} Q$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} i \frac{R_2}{z^2 (zR_2 - a^2 e^{i p})} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i p}} \frac{R_2}{z^2} Q$$

$$a_{94} = Res_1 - Res_2 = 0$$

Para a_{95}

$$f(z) = i \frac{R_2}{(zR_2 - a^2 e^{i p})} V_o$$

$$Res = \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(i \frac{R_2}{(zR_2 - a^2 e^{i p})} V_o \right) \right) = i \frac{R_2}{z^2} V_o$$

$$a_{95} = i \frac{R_2}{z^2} V_o$$

Para a_{96}

$$f(z) = -i \frac{R_2}{(zR_2 - a^2 e^{i p})} V_o \frac{a^2}{z^2}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-i \frac{R_2}{(zR_2 - a^2 e^{i p})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{i}{a^2 e^{2 i p}} R_2^2 \frac{a^2}{z^2} V_o$$

$$Res_2 = \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(-i \frac{R_2}{(zR_2 - a^2 e^{i p})} V_o \frac{a^2}{z^2} \right) \right) = \frac{i}{a^2 e^{2 i p}} R_2^2 \frac{a^2}{z^2} V_o$$

$$a_{96} = Res_1 - Res_2 = 0$$

Para a_{97}

$$f(z) = -\frac{1}{2} \frac{R_2}{z^2 (zR_2 - a^2 e^{i p})} \frac{Q}{z}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i p}}{R_2}} \left(\left(z - \frac{a^2 e^{i p}}{R_2} \right) \left(-\frac{1}{2} \frac{R_2}{z^2 (zR_2 - a^2 e^{i p})} \frac{Q}{z} \right) \right) = \frac{1}{2a^2 e^{i p}} \frac{R_2}{z^2}$$

$$Res_2 \quad \lim_{z \rightarrow 0} \left(z - 0 \left(-\frac{1}{2} \frac{R_2}{z R_2 a^2 e^{i p}} \frac{1}{z} \right) \right) - \frac{1}{2 a^2 e^{i p}} \frac{R_2}{2}$$

$$a_{97} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{98}

$$f(z) = -\frac{1}{2} \frac{z^{\frac{2}{2}}}{z R_2 e^{i p}} \frac{R_2}{a^2 e^{i n}}$$

$$Res \quad \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-\frac{1}{2} \frac{z^{\frac{2}{2}}}{z R_2 e^{i p}} \frac{R_2}{a^2 e^{i n}} \right) \right) = \frac{1}{2(a^2 e^{i n} - R_2^2 e^{i p})} \frac{z^{\frac{2}{2}}}{2} R_2$$

$$a_{98} = \frac{1}{2(a^2 e^{i n} - R_2^2 e^{i p})} \frac{z^{\frac{2}{2}}}{2} R_2$$

Para a_{99}

$$f(z) = -i R_2 \frac{z^2}{(z R_2 a^2 e^{i n})} V_o$$

$$Res \quad \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(-i R_2 \frac{z^2}{(z R_2 a^2 e^{i n})} V_o \right) \right) = -i \frac{z^2}{2} V_o$$

$$a_{99} = -i \frac{z^2}{2} V_o$$

Para a_{100}

$$f(z) = i R_2 \frac{z^2}{(z R_2 a^2 e^{i n})} V_o \frac{a^2}{z^2}$$

$$Res_1 \quad \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(i R_2 \frac{z^2}{(z R_2 a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = \frac{i}{a^2 e^{2 i n}} R_2^2 \frac{z^2}{2} V_o$$

$$Res_2 \quad \frac{1}{2-1!} \lim_{z \rightarrow 0} \frac{d^{2-1}}{dz^{2-1}} \left(z - 0 \left(i R_2 \frac{z^2}{(z R_2 a^2 e^{i n})} V_o \frac{a^2}{z^2} \right) \right) = -\frac{i}{a^2 e^{2 i n}} R_2^2 \frac{z^2}{2} V_o$$

$$a_{100} \quad Res_1 \quad Res_2 \quad 0$$

Para a_{101}

$$f(z) = \frac{1}{2} R_2 \frac{2}{z^2 (z R_2 a^2 e^{i n})} \frac{1}{z}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(\frac{1}{2} R_2 \frac{2}{z^2 (z R_2 a^2 e^{i n})} \frac{1}{z} \right) \right) = -\frac{1}{2 a^2 e^{i n}} R_2^{-\frac{2}{2}}$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} R_2 \frac{2}{z^2 (z R_2 a^2 e^{i n})} \frac{1}{z} \right) \right) = \frac{1}{2 a^2 e^{i n}} R_2^{-\frac{2}{2}}$$

$$a_{101} = Res_1 + Res_2 = 0$$

Para a_{102}

$$f(z) = i V_o \frac{1}{z}$$

$$Res = \lim_{z \rightarrow 0} (z - 0) i V_o \frac{1}{z} = i V_o$$

$$a_{102} = i V_o$$

Para a_{103}

$$f(z) = -V_o \frac{Q}{z}$$

$$Res = \lim_{z \rightarrow 0} \left(z - 0 \left(-V_o \frac{Q}{z} \right) \right) = -V_o \frac{Q}{z}$$

$$a_{103} = -V_o \frac{Q}{z}$$

Para a_{104}

$$f(z) = -\frac{1}{4} R_2^2 \frac{\frac{2}{2}}{z^2 (z R_2 a^2 e^{i n})^2}$$

$$Res = \frac{1}{2-1!} \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \frac{d^{2-1}}{dz^{2-1}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right)^2 \left(-\frac{1}{4} R_2^2 \frac{\frac{2}{2}}{z^2 (z R_2 a^2 e^{i n})^2} \right) \right) = 0$$

$$a_{104} = 0$$

Para a_{105}

$$f(z) = \frac{1}{2} i R_2 \frac{2}{z R_2 a^2 e^{i n}} \frac{Q}{z}$$

$$Res_1 = \lim_{z \rightarrow -\frac{a^2 e^{i n}}{R_2}} \left(\left(z - \frac{a^2 e^{i n}}{R_2} \right) \left(\frac{1}{2} i R_2 \frac{2}{z R_2 a^2 e^{i n}} \frac{Q}{z} \right) \right) = -\frac{1}{2} \frac{i}{a^2 e^{i n}} R_2 \frac{2}{2} Q$$

$$Res_2 = \lim_{z \rightarrow 0} \left(z - 0 \left(\frac{1}{2} i R_2 \frac{2}{z R_2 a^2 e^{i n}} \frac{Q}{z} \right) \right) = \frac{1}{2} \frac{i}{a^2 e^{i n}} R_2 \frac{2}{2} Q$$

$$a_{105} \quad Res_1 \quad Res_2 \quad 0$$